Energy-Efficient Algorithms

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Motivation

Energy is scarce and/or expensive resource.

- Limited availability: Portable, battery-operated devices; sensor networks.

Motivation

- Electricity cost: substantial strain for computing and data centers
  Google: 1 billion $ per year

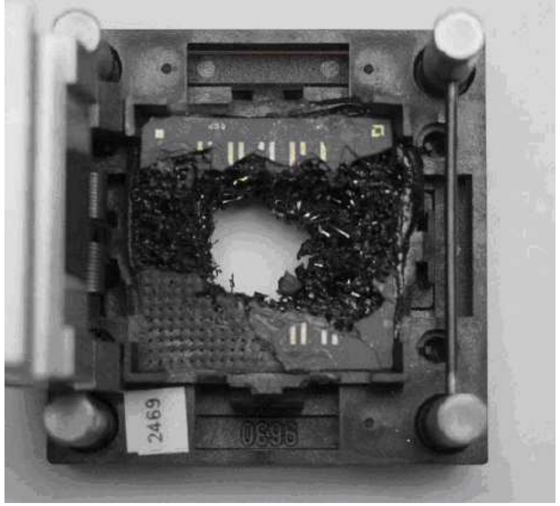
  "What matters most [...] at Google is not speed, but power, low power because data centers can consume as much electricity as a city." Eric Schmidt, *NYT* 2002

  Google uses enough electricity to power 200.000 homes. *NYT* 2011

  Low-cost power major criterion where to build data centers. Apple, Facebook, Google

Motivation

- Thermal problems: Most of the energy is converted into heat.



Energy-efficient algorithms

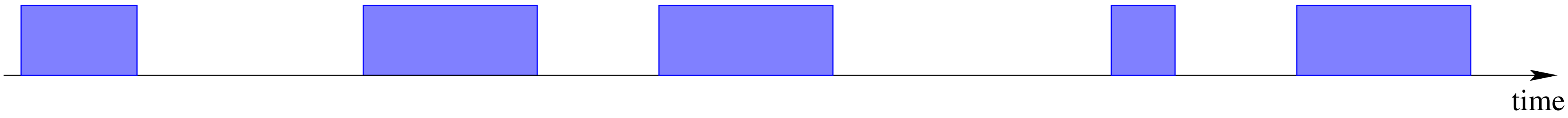
Topics

- Power-down mechanisms: Transition system into sleep state when idle
- Dynamic speed scaling: Microprocessors can run at variable speed
  Intel XScale, Intel Speed Step, AMD PowerNow
- Networks: Optimize transmission energy

Power-down strategies

2-state system

- Active state: r energy units per time unit.
- Sleep state: 0 energy units per time unit.
- Wake-up operation: W energy units.
- When active period starts, system must be in / moved to active state.



Right-sizing in data centers

m heterogeneous servers

active state

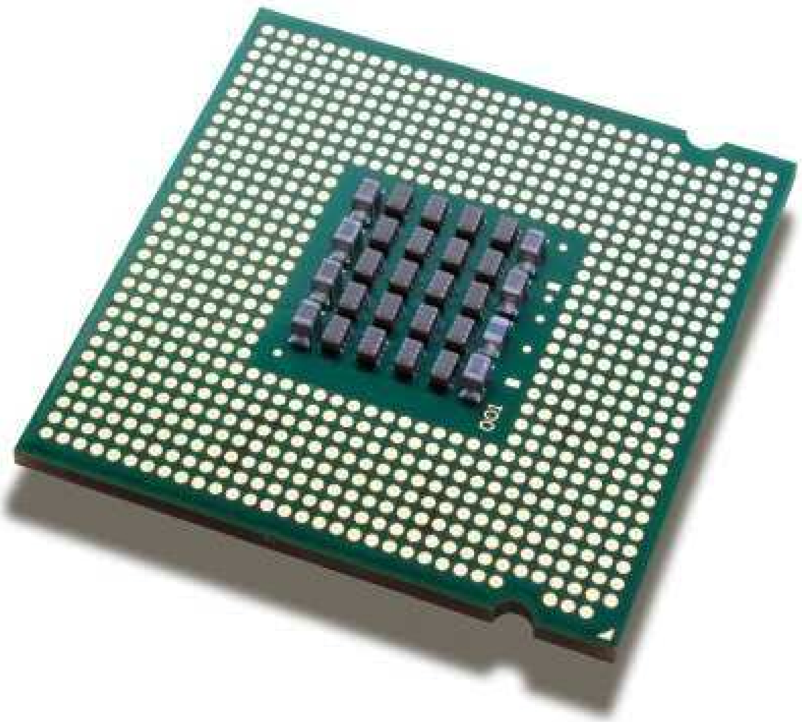
standby and sleep states

Demand for computing capacity varies over time

Dynamic speed scaling

Variable-speed microprocessors

Intel XScale, Intel Speed Step, AMD PowerNow



The higher the speed, the higher the energy consumption

Speed s

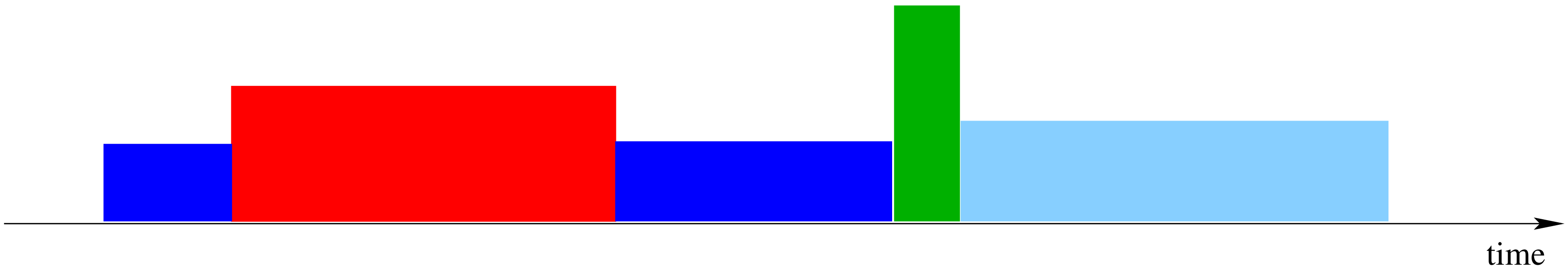
Power required

$P(s) = s^{\alpha} \quad \alpha > 1$

$P(s)$ = general convex function

Scheduling with deadlines

1 processor



- Speed s Power consumption $P(s) = s^\alpha$ $\alpha > 1$
- $\sigma = J_1, \ldots, J_n$
  J_i: a_i = arrival time
  b_i = deadline
  v_i = processing volume $t = v_i / s$
- Preemption allowed
- Construct feasible schedule minimizing total energy consumption.

Yao, Demers, Shenker FOCS'95

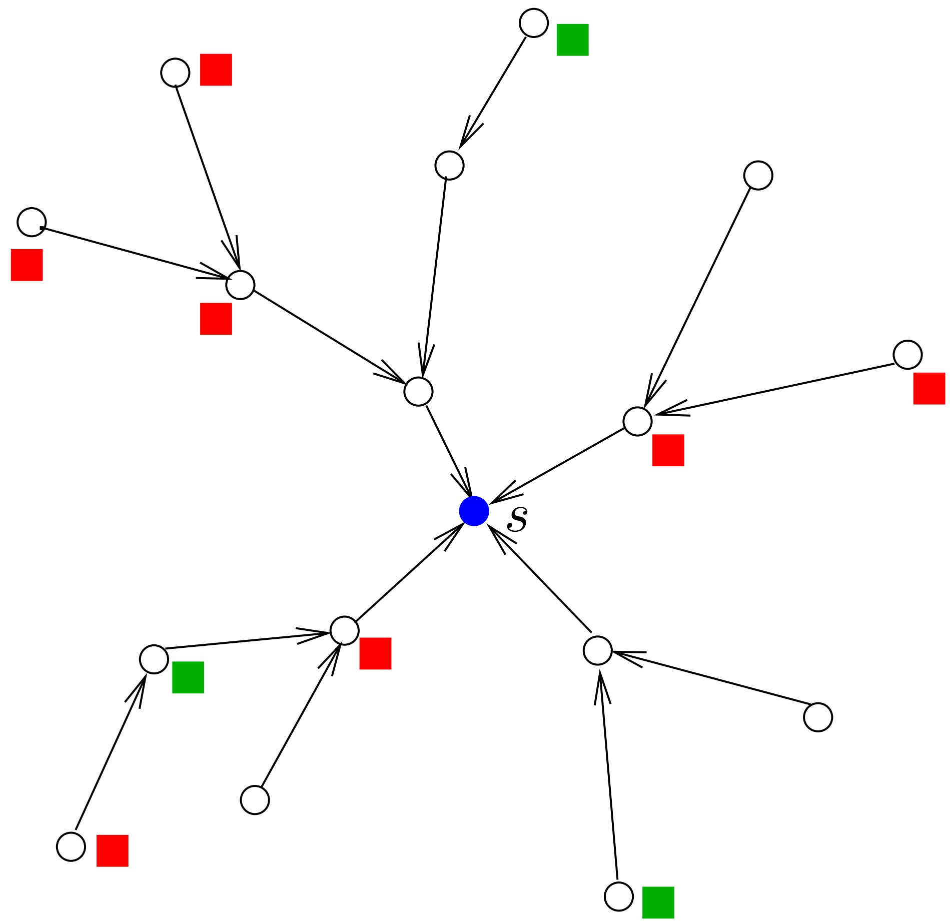
Data aggregation

Tree topology

Data (packets) to be sent to sink

Pakets may be aggregated

Energy: 1 per sending operation



Topics

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